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Edition 3.0 2014-01

TECHNICAL REPORT

colour inside

Optical fibres – Reliability – Power law theory

IEC TR 62048:2014-01(EN)

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TECHNICAL REPORT

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Optical fibres – Reliability – Power law theory

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OPTICAL FIBRES –

Reliability – Power law theory

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IEC/TR 62048, which is a technical report, has been prepared by subcommittee 86A: Fibres and cables, of IEC technical committee 86: Fibre optics.

This third edition cancels and replaces the second edition published in 2011, and constitutes a technical revision.

The main changes with respect to the previous edition are listed below:

– correction to the unit of failure rates in Table 1;

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– correction to the FIT equation for instantaneous failure rate [19][1] in addition to all call-outs and derivations;
– insertion of a new note about fibre length dependency of failure rates;
– addition of informative Annex A and relevant reference;
– editorial corrections of inconsistencies.

The text of this technical report is based on the following documents:

Enquiry draft	Report on voting
86A/1537/DTR	86A/1554/RVC

Full information on the voting for the approval of this technical report can be found in the report on voting indicated in the above table.

This publication has been drafted in accordance with the ISO/IEC Directives, Part 2.

The committee has decided that the contents of this publication will remain unchanged until the stability date indicated on the IEC web site under "http://webstore.iec.ch" in the data related to the specific publication. At this date, the publication will be

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- withdrawn,
- replaced by a revised edition, or
- amended.

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IMPORTANT – The 'colour inside' logo on the cover page of this publication indicates that it contains colours which are considered to be useful for the correct understanding of its contents. Users should therefore print this document using a colour printer.

[1] Numbers in square brackets refer to the Bibliography.

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INTRODUCTION

Reliability is expressed as an expected lifetime or as an expected failure rate. The results cannot be used for specifications or for the comparison of the quality of different fibres. This technical report develops the theory behind the experimental principles used in measuring the fibre parameters needed in the reliability formulae. Much of the theory is taken from the referenced literature and is presented here in a unified manner. The primary results are formulae for lifetime or for failure rate, given in terms of the measurable parameters. Conversely, an allowed maximum service stress or extreme value of another parameter may be calculated for an acceptable lifetime or failure rate.

For readers interested only in the final results of this technical report – a summary of the formulae used and numerical examples in the calculation of fibre reliability – Clauses 6 and 7 – are sufficient and self-contained. Readers wanting a detailed background with algebraic derivations will find this in Clauses 8 to 12. An attempt is made to unify the approach and the notation to make it easier for the reader to follow the theory. Also, it should ensure that the notation is consistent in all test procedures. The Bibliography has a limited set of mostly theoretical references, but it is not necessary to read them to follow the analytical development in this technical report. Annex A introduces a statistical strength degradation (SSD) map which gives intuitive understanding of the physical meaning of the formulae appearing in Clauses 10 and 11.

NOTE Clauses 8 to 12 reference the B-value, and this is done for theoretical completeness only. There are as yet no agreed methods for measuring B, so the Bibliography gives only a brief analytical outline of some proposed methods and furthermore develops theoretical results for the special case in which B can be neglected.

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OPTICAL FIBRES –

Reliability – Power law theory

1 Scope

This technical report is a guideline that gives formulae to estimate the reliability of fibre under a constant service stress based on a power law for crack growth.

NOTE Power law is derived empirically, but there are other laws which have a more physical basis (for example, the exponential law). All these laws generally fit short-term experimental data well but lead to different long-term predictions. The power law has been selected as a most reasonable representation of fatigue behaviour by the experts of several standard-formulating bodies.

2 Normative references

The following documents, in whole or in part, are normatively referenced in this document and are indispensable for its application. For dated references, only the edition cited applies. For undated references, the latest edition of the referenced document (including any amendments) applies.

IEC 60793-1-30, *Optical fibres – Part 1-30: Measurement methods and test procedures – Fibre proof test*

IEC 60793-1-31, *Optical fibres – Part 1-31: Measurement methods and test procedures – Tensile strength*

3 Symbols

Table 1 provides a list of symbols found in this report. Each symbol appears in the subclause(s) indicated in the final column of the table.

Table 1 – Symbols

Symbol	Unit	Name	Subclause
a	µm	Flaw depth	8.1
a_f	µm	Radius of glass fibre	11.3
B	GPa^2×s	Crack strength preservation parameter or B-value	8.1
B_0	GPa^2×s	Transitional B-value at the slow-unloading/fast-unloading boundary	10.4
c	Dimensionless	Non-linearity term for stress versus strain	8.4
C	Dimensionless	Additive dimensionless proof test term or C-value	11.6
C_0	Dimensionless	Transitional value of C at the slow-unloading/fast-unloading boundary	11.6
D	Mm	Fibre-axes separation in two-point bending	11.3.3
E_0	Gpa	Zero-strain Young's modulus	8.4
F	Dimensionless	Fibre failure probability	12.1
$K_I(t)$	GPa×µm$^{1/2}$	Stress intensity factor	8.1
K_{Ic}	GPa×µm$^{1/2}$	Critical stress intensity factor	8.1

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Symbol	Unit	Name	Subclause
L	km	Fibre effective length under uniform stress, or equivalent tensile length	11.2.1
L_b	km	Fibre length in uniform bend	11.3.2
L_p	km	Mean survival length, or survival length, during proof-testing	11.6
L_0	km	Gauge length, reference length	11.2.1
m	Dimensionless	"Inert" Weibull parameter or m-value	11.2.1
m_d	Dimensionless	m-value under dynamic fatigue	11.5
m_s	Dimensionless	m-value under static fatigue	11.4
n	Dimensionless	Stress corrosion susceptibility parameter or n-value	6.3, 8.1
N_p	km^{-1}	Mean break rate per unit length during proof-testing	11.6
$N(S)$	km^{-1}	Flaws per unit length not exceeding inert strength S	11.2.1
P	Dimensionless	Fibre survival probability	11.2.1
P_p	Dimensionless	Fibre survival probability after proof-testing	11.6
R	M	Fibre bend radius	11.3.2
$S(t)$	GPa	"Inert" strength of a crack	8.1
S_p	GPa	Strength after proof-testing	10.3
S_{pmin}	GPa	Minimum strength after proof-testing	10.4
S_0	GPa	Weibull gauge strength	11.2.1
t	s	Variable of time	8.1
t_d	s	Time to failure under dynamic fatigue	8.3.2
		Dwell time of proof test	6.3.2, 6.4.2, 10.2, 10.3
t_f	s	Lifetime (time to failure) under constant stress or static fatigue testing	8.2, 9.2
t_{fp}	s	Lifetime after proof-testing	11.8
t_{fpmin}	s	Minimum lifetime for certain survival after proof-testing	11.8
$t_f(1)$	Dimensionless	Intercept on a static fatigue plot	9.2
t_l	ms	Loading time of proof test	10.2
t_p	ms	Effective proof test time	10.3
t_u	ms	Unloading time of proof test	10.2
t_0	Dimensionless	Static Weibull time-scaling parameter	11.4
V	µm/s	Crack growth velocity	8.1
V_C	µm/s	Critical crack growth velocity	8.1
x	Dimensionless	Factor relating bend length to equivalent tensile length	11.3.2
Y	Dimensionless	Crack geometry shape parameter	8.1
α	Dimensionless	Ratio of unloading parameters of proof test to crack parameters	10.4
β	$GPa^n \times s \times km^{(n-2)/m}$	Weibull β-value	11.4, 11.5
ε	Dimensionless	Strain corresponding to a particular stress	8.4
λ_i	s^{-1}	Instantaneous failure rate	12.1
λ_a	s^{-1}	Averaged failure rate	12.2
$\sigma(t)$	GPa	Stress applied to a crack	8.1
σ_a	GPa	Applied stress under static fatigue testing and service time	9.2, 12.2
$\dot{\sigma}_a$	GPa/s	Applied stress rate under dynamic fatigue testing	8.3.2

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Symbol	Unit	Name	Subclause
σ_f	GPa	Failure stress under dynamic fatigue testing, without proof-testing	8.3.2
σ_{fp}	GPa	Failure stress after proof-testing	11.8
σ_{fpmin}	GPa	Minimum failure stress after proof-testing	11.8
$\sigma_f(1)$	Dimensionless	Intercept on a dynamic fatigue plot	8.3.2
σ_p	GPa	Proof test stress	10.2
σ_0	GPa	Dynamic Weibull stress-scaling parameter	11.5

4 General approach

First, the equivalence of the growth of an individual crack and its associated weakening is shown. This is related to applied stress or strain as an arbitrary function of time. Applied stress can be taken to fracture, from which the lifetime of the crack is calculated. Next, the destructive tests of static and dynamic fatigue are reviewed, along with their relationship to each other. These tests measure parameters useful in the theory. This also shows the difference between "inert" strength and "dynamic" strength.

The above single-crack theory is then extended to a statistical distribution of many cracks. This is done in terms of a survival (or failure) Weibull probability distribution in strength. It can allow for several deployment geometries in testing and service. The inert distribution and the distributions obtained by static or dynamic fatigue testing are derived for before and after proof-testing. The latter is sometimes done with approximations that may not require knowing the B-value explicitly. Finally, the various parameters measured by the above testing are related to formulae for fibre reliability, that is, lifetime and failure rate.

Some of the main assumptions in the development are as indicated below.

– The relationship between the stress intensity factor, applied stress, and flaw size is given by Equation (29); while at fracture, the relationship between the critical stress intensity factor, strength, and flaw depth is given by Equation (30).
– The crack growth velocity is related to the stress intensity factor by Equation (32).
– The Weibull distribution of stress (before any proof-testing) is unimodal according to Equations (85) and (86), or bimodal according to Equation (91). The (m, S_0) pair appropriate to the desired survival probability level and length shall be used. Deployment lengths will differ upon the application such as fibre on reels, in cable, splice trays, or within a connector or other component. Because of the low failure probabilities desired, however, the low-strength extrinsic mode must usually be used.
– The values of the fatigue parameters, both static and dynamic, depend upon the fibre environment, fibre ageing and fibre preconditioning prior to testing. In theory, they are taken to be independent of time, so that some engineering judgement is needed to decide the practical values to be used in the calculations. This also implies that the corresponding static and dynamic fatigue parameters equal each other (for the same environment and time duration).
– Zero-stress ageing is not accounted for. Since the above parameters are independent of time, the strength decreases due only to stress fatigue following the power law according to 8.1.

5 Formula types

The formulae utilize parameters obtained from fatigue testing-to-failure, and from proof-testing with potential random failures. In the service condition of interest, a fibre of effective length L (dependent upon deployment geometry) is subjected to a constant applied service stress that does not change with time. (This stress is tensile, including bending stress. Torsional or

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compressive stresses are not covered.) The lifetime as a function of failure probability or failure rate as a function of time are given.

The formulae assume a Weibull distribution with parameters that vary among fibre types and perhaps among fibres of the same type. Moreover, they change with environment and applied stress levels. The Weibull distribution may have several nominally linear terms depending upon several levels of flaw strength. It is important that the Weibull parameters for the term of interest be used in the formulae. These are obtained from fatigue measurements. Generally, the low-strength region near the proof test stress and below is of interest, and measurements shall be on long fibre gauge lengths and with many samples, so that the total fibre length tested is large. Parameters measured for a small number of short samples, characterizing the high-strength region, will differ from the preceding ones. They shall not be used in the formulae to extrapolate to lower-strength lower-probability regions.

Within the above power law assumptions, the equations in Clauses 8 to 12 are algebraically "exact". However, in some applications, certain terms may be negligible, and more approximate and simpler algebraic equations are given in Clause 13. This has the advantage in that the B-value, for which there is yet no standard test method and which has been reported to span several orders of magnitude, is not required.

Even with these formulae, there is no assured way of accurately predicting fibre reliability. Some fibres may break before the most conservative of predictions, while others may last longer than the most pessimistic of predictions. After fibre manufacture, fatigue or damage may occur due to cabling, installation, or operation; this usually cannot be accounted for in the theory. A start on estimating these effects could be made by measuring the parameters of fibres after each of these stages, but this is not commonly done.

For convenience in assisting the reader to find the derivations of equations, if desired, the formulae summarized in Clauses 6 and 7 include the indication in brackets of the equations listed in Clauses 8 to 13. However, it is not necessary to refer to the derivations to be able to follow Clauses 6 and 7.

6 Measuring parameters for fibre reliability

6.1 Overview

This clause outlines how the parameters in the reliability (lifetime and failure rate) equations are obtained in the approximation of the small B-value. Proof test parameters are obtained from testing the full length of fibre to be deployed. By contrast, both static and dynamic fatigue procedures use many short-length test samples. These are used to obtain "linear" Weibull plots of the cumulative failure probability F scaled as ln-ln $\frac{1}{P}$ (where $P = 1 - F$ is the survival probability) versus the ln of a suitable variable (failure time or failure stress). For situations in which the plot may be fitted to two or more straight line parts, that part closest to the anticipated service stress should be used in obtaining the needed parameters.

6.2 Length and equivalent length

The testing and service geometries may differ from each other. The symbol L_0 is the gauge length in static or dynamic fatigue testing, whereas L is the in-service length subjected to constant applied service stress. The gauge length equals the actual length only for the case of longitudinal tension. Other geometries require equivalent lengths.

For uniform bending (for example, mandrel wrap), the in-service bend length L_b is replaced by an approximate equivalent in-service tensile length L given by Equation (97).

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$$L \approx 0{,}4 \frac{L_b}{\sqrt{x}} \tag{1}$$

The same relationship holds between the gauge bend length L_{b0} and the equivalent gauge length L_0. In this equation there is the factor of Equation (98), i.e.

$$x = \frac{mn}{n-2} = m_s n = \frac{m_d n}{n+1} \tag{2}$$

using inert, static fatigue, and dynamic fatigue parameters, respectively, as obtained below.

For two-point bending, the equivalent length depends upon the applied stress in a complex way. Computation of the equivalent in-service length for an arbitrary applied service stress is difficult. The equivalent gauge length is approximately 10 μm to 30 μm, depending upon the failure stress.

6.3 Reliability parameters

6.3.1 Overview

This subclause outlines methods that are commonly used to derive reliability parameters.

6.3.2 Proof-testing

– Obtain the composite proof test parameter $\sigma_p^n t_p$, where σ_p is the actual proof test stress during dwell, and n is the stress-corrosion susceptibility parameter (or n-value). The effective proof test time is given by Equation (64), i.e.

$$t_p = t_d + \frac{t_l + t_u}{n+1} \tag{3}$$

obtained from the loading time t_l, the dwell time t_d, and the unloading time t_u.

– (Optional) If from proof-testing the mean number of breaks N_p per length or the mean survival length L_p during proof-testing is known, calculate Equations (172) and (173), i.e.

$$\beta = \frac{\sigma_p^n t_p}{N_p^{\frac{n-2}{m}}} = \sigma_p^n t_p L_p^{\frac{n-2}{m}} \tag{4}$$

$$\text{where } \frac{m}{n-2} = m_s = \frac{m_d}{n+1} \tag{5}$$

If this is not possible, obtain β as a fitting parameter in 6.3.3, 6.3.4, or 6.4.

6.3.3 Static fatigue

– Obtain the static Weibull plot of scaled probability versus the natural logarithm of failure times t_f for any particular constant applied stress σ_a [Equation (174)]

$$\ln \frac{1}{P_p(t_f)} = \left[\left(t_f \sigma_a^n + t_p \sigma_p^n \right)^{m_s} - \left(t_p \sigma_p^n \right)^{m_s} \right] \frac{L}{\beta^{m_s}} \tag{6}$$

– Determine parameters ms and β from the characteristics of the plot.

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– Obtain the best-fit straight line to the logarithm of failure times versus the logarithm of applied stresses (see Equation (48))

$$\lg t_f(\sigma_a) \approx \lg t_f(1) - n \lg \sigma_a \tag{7}$$

Measure the static stress-corrosion susceptibility parameter as the negative slope $-n$ of this line. The term $t_f(1)$ is the "intercept" of this line on the ordinate axis, that is, the value of failure time where the applied stress is unity. (This value will depend on the units used, and may require a straight-line extrapolation beyond the data points. It does not have the dimension of time.)

6.3.4 Dynamic fatigue

IEC 60793-1-31 describes how to measure both short-length and long-length strength distributions of optical fibres.

– Obtain the dynamic Weibull plot of scaled probability versus the natural logarithm of failure stresses σ_f for any particular constant applied stress rate $\dot{\sigma}_a$ (see Equation (175))

$$\ln \frac{1}{P_p(\sigma_f)} = \left\{ \left[\frac{\sigma_f^{n+1}}{(n+1)\dot{\sigma}_a} + \sigma_p^n t_p \right]^{\frac{m_d}{n+1}} - \left(\sigma_p^n t_p\right)^{\frac{m_d}{n+1}} \right\} \frac{L}{\beta^{\frac{m_d}{n+1}}} \tag{8}$$

Determine parameters m_d and β from the characteristics of the plot.

– Obtain the best-fit straight line to the logarithm of failure stresses versus the logarithm of applied stress rates, as given in Equation (53):

$$\lg \sigma_f(\dot{\sigma}_a) \approx \lg \sigma_f(1) + \frac{\lg \dot{\sigma}_a}{n+1} \tag{9}$$

Measure the dynamic stress-corrosion susceptibility parameter from the slope $\frac{1}{n+1}$ of this line.

The term $\sigma_f(1)$ is the "intercept" of this line on the ordinate axis, that is, the value of failure stress where the applied stress rate is unity. (This value will depend on the units used, and may require a straight-line extrapolation beyond the data points. It does not have the dimension of stress.)

6.4 Parameters for the low-strength region

6.4.1 Overview

This subclause describes the way to measure the strength distribution at sufficiently low probability to represent the distribution of failure strengths near the proof test stress level for the second mode of the Weibull distribution (shown as the extrinsic region in Figure 14). Normally, the fibre population has been proof-tested once according to Clause 10.

NOTE These implementations are used only for characterization and not for specification.

6.4.2 Variable proof test stress

This method (briefly mentioned in 10.5) subjects a full length of fibre to a certain proof test stress, another length to a higher proof test stress, and so on for several increasing levels of

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proof test stress. The mean survival length L_p (or number of breaks N_p per unit length) is counted for each length and stress level. This resembles a static fatigue test in which the failure stress (the proof test stress σ_p) varies. However, the failure time does not exceed the fixed proof test time t_p. The n-values are obtained by the fatigue measurements of 6.3.

First, consider the case in which there is no initial proof test at manufacture. From Equations (171) and (173) one has

$$\ln L_p + m_s(n \ln \sigma_p + \ln t_p - \ln \beta) = 0 \tag{10}$$

so a logarithmic plot of mean survival length versus proof test stress should be close to a straight line. The slope is $-nm_s$, while the stress and length "intercepts" are $\frac{1}{n}(\ln \beta - \ln t_p)$ and $m_s(\ln t_p - \ln \beta)$, respectively.

In Reference [11], fibres with a 400 μm jacket and initial lengths of 10 km to 15 km were used, with five proof test strains of 0,8 % to 3,5 %. There was no other initial proof test. Equation (10) is equivalent to Equations (18) to (20) of Reference [11] with $C = \beta^{-m_s}$. With a dwell time t_d of 1 s, it was found that nm_s = 2,07, so that with n = 20, one has m_s = 0,1035. Also, $m_s \ln t_p + \ln C = -2{,}09$, so that $\beta^{m_s} = 8{,}085$ GPa$^{nm_s} \cdot$ s$^{m_s} \cdot$km.

More common is the case in which there is an initial proof test at manufacture. If the second proof test stress is significantly above the first, then Equation (10) can still be used.

In Reference [12], the proof test stress level at manufacture was not stated. A minimum sample length of 10 km or 20 km was used, and each sample was subjected to a different one of five proof test stress levels between 1 GPa and 4 GPa. The proof test speed was reduced to minimize breakage during the start-up acceleration period, so the dwell time t_d was normalized to 1 s using n = 23. The failure probabilities F per meter were calculated for each stress and plotted to fit the straight line of the form

$$\ln\left(\frac{1}{1-F}\right) = M \ln \sigma_p + \ln K \tag{11}$$

With another "ln" on the left (apparently missing), this is equivalent to Equation (101) for static fatigue (ignoring the initial proof-testing) if

$$M \equiv nm_s \text{ and } K \equiv \left(\frac{t_d}{\beta}\right)^{m_s} \tag{12}$$

From this it was determined that M = 1,69, so we find m_s = 0,0735, and K = 0,000418, so that $\beta^{m_s} = 2{,}392$ GPa$^{nm_s} \cdot$ s$^{m_s} \cdot$km.

6.4.3 Dynamic fatigue

6.4.3.1 Overview

This is a form of dynamic fatigue testing with censoring, as mentioned in 9.3.3, and with more details on the apparatus given in Reference [5].

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6.4.3.2 Data acquisition of dynamic fatigue

A specimen is a single gauge length L_0 of fibre. (A recommended gauge length L_0 is longer than 1 m; for example, 10 m to 20 m.) A sample is a group of specimens from a given population of fibres.

Each specimen is loaded to a failure stress σ_f, or, with censoring, to a (non-failing) maximum stress σ_{max} (for example, 2,4 GPa, about 3,2 % strain from Equation (44)). The recommended strain rate $\dot{\sigma}_a$ is fast (for example, greater than 200 %/min, about 2,6 GPa/s, from Equation (43)). The sample size should be large enough to provide an adequate representation of the second Weibull mode (for example, so that 1 km of the total specimens fail).

The following data are recorded:

– the total number of specimens tested: N, whether or not failure occurred;

– the failure stress values of those specimens that failed: σ_{fi} in GPa. Here i is the rank order, sorted by increasing failure stress.

– the stress rate (converted from strain rate): $\dot{\sigma}_a$ in GPa/s.

– the gauge length of the specimens: L_0 in km.

A Weibull plot in the form of Figure 1 may also be presented (without the curve fittings). The points are measurements from about 0,8 GPa to 2,4 GPa, for an acrylate-coated fused silica fibre with a cladding diameter of 125 μm.

6.4.3.3 Calculation of Weibull parameters

Here the data of the measurement is analysed. According to Equation (86), the Weibull cumulative probability ordinate scale is of the form

$$\ln\left[\ln\left(\frac{1}{1-F}\right)\right],$$

where $F = 1 - P$ is the cumulative failure probability.

Hence compute

$$w_i = \ln\left[-\ln\left(1-\frac{i}{N+1}\right)\right] \tag{13}$$

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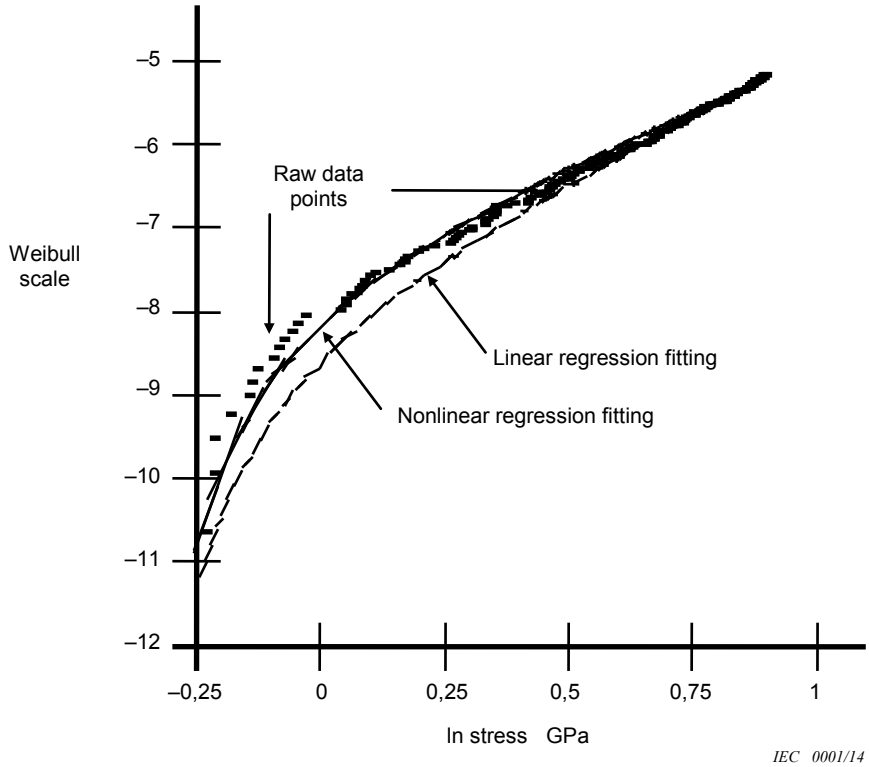

Figure 1 – Weibull dynamic fatigue plot near the proof test stress level

Exponentiate this and use a rearranged form of an approximation (175) of Equation (138)

$$\exp w_i = \frac{\sigma_{fi}^{m_d} L_0}{\left[\dot{\sigma}_a (n+1)\beta\right]^{\frac{m_d}{n+1}}} \times \left\{ \left[1 + \frac{\dot{\sigma}_a (n+1)\sigma_p^n t_p}{\sigma_{fi}^{n+1}} \right]^{\frac{m_d}{n+1}} - \left[\frac{\dot{\sigma}_a (n+1)\sigma_p^n t_p}{\sigma_{fi}^{n+1}} \right]^{\frac{m_d}{n+1}} \right\} \tag{14}$$

Here the length L becomes the testing gauge length L_0.

Two fittings are used on this equation.

a) Linear regression fitting

For large failure stresses, the term in Equation (14) that is enclosed in curled brackets { } approaches one. The equation approaches the "linear" form of the usual Equations (108) and (110) without proof-testing

$$w_i = A + m_d \ln \sigma_{fi} \tag{15}$$

where

$$\ln \beta = \frac{n+1}{m_d}(\ln L_0 - A) - \ln\left[(n+1)\dot{\sigma}_a\right] \tag{16}$$

Hence for failure stress greater than some selected value, find m_d and A such that the least squares error of w_i is minimized.

This procedure produces the linear regression fitting in Figure 1. Clearly, it would be better to have a closer fit at the left side of this data set, where the values are closer to the applications of interest.

b) Non-linear regression fitting

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This uses lower-stress data, where the curvature is apparent. Given a value of m_d, a value of β is computed for each failure stress, and a value from the middle of the data of interest produces a curve that goes through that area. The result produces a sum of squared errors for the entire curve, and m_d is varied to minimize the sum. The steps are indicated below.

– Define a range of data in which the fitting is to be forced. Here it is constructed using ln σ_{fi} values between 0 and 0,5.
– Select a value of m_d.
– Compute ln β_i for each failure stress in the defined region using Equation (14).
– Set ln β equal to the median of the computed ln β_i values.
– Compute $wout_i$ using Equation (14) and the above value of β.
– Compute the squared errors $(w_i - wout_i)^2$, and then compute the sum of squared errors.
– Vary m_d as in the second step, and repeat the remaining steps to minimize the sum.

The procedure produces the non-linear regression fitting in Figure 1.

6.5 Measured numerical values

In this subclause, experimental values resulting from the measurements of 6.4.3 are obtained. They will be used in the calculations of Clause 7.

In 6.3.2, the composite proof test parameter is $\sigma_p^n t_p = 8{,}8849 \times 10^{-5}$ GPa^n·s, with a nominal proof-stress of σ_p = 0,69 GPa (ln σ_p = –0,37 in Figure 1). From 6.3.4 n = 20 is obtained, and in 6.4.3 the stress rate is $\dot{\sigma}_a$ = 4,59477 GPa/s for a gauge length L_0 = 20 m. The non-linear fitting gives the values m_d = 2,359 and ln β = 25,499. Note that β has the unit $\mathrm{GPa}^n \cdot \mathrm{s} \cdot \mathrm{km}^{\frac{n+1}{m_d}}$.

The static value will also be needed in the following subclause (see Equation (114)):

$$m_s = \frac{m_d}{n+1} \tag{17}$$

which according to the above subclause equals 0,11233. Note too that β now has the unit $\mathrm{GPa}^n \cdot \mathrm{s} \cdot \mathrm{km}^{\frac{1}{m_s}}$ and that β^{m_s} = 17,538 $\mathrm{GPa}^{nm_s} \cdot \mathrm{s}^{m_s} \cdot \mathrm{km}$.

The two values are in reasonable agreement with those of 6.4.2.

7 Examples of numerical calculations

7.1 Overview

The numerical values experimentally obtained in 5.5 are used in the calculations below. The results will be conservative since the explicit B-value is neglected; lower failure rates and longer lifetimes would be obtained if this value were included. (The degree of improvement increases as B increases.) The results of the calculations can be quite sensitive to the choice of parameter values. These values are related to each other, and a change in one parameter will affect the values of other parameters. Ideally, the parameter values should be obtained on the basis of experimentation.

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If the failure probability $F = 1 - P$ is 10^{-3} or less (generally the region of practical interest), the term $\ln\frac{1}{P}$ in the formulae below may be replaced by F to an accuracy of 0,5 % or better, but this has not been done in the numerical results given here. See Equation (160)

$$t_f(\text{sec}) = 31\ 557\ 600\ t_y(\text{yr}) \tag{18}$$

7.2 Failure rate calculations

Compute the failure rates λ that would occur at various static stress levels σ_a as a function of service time t_y in years.

7.2.1 FIT rate formulae

The instantaneous failure rate in FIT is (see Equation (178)):

$$\lambda_i\left(t_f\right) = 3{,}6\times10^{12} m_s L\left(\frac{\sigma_a^n}{\beta}\right)^{m_s}\left[t_f + t_p\left(\frac{\sigma_p}{\sigma_a}\right)^n\right]^{m_s-1} \tag{19}$$

The averaged failure rate in FIT is [Equation (179)]

$$\lambda_a(t_f) = \frac{3{,}6\times10^{12}}{t_f}\left\langle 1-\exp\left\{\left[\left(t_p\sigma_p^n\right)^{m_s} - \left(t_f\sigma_a^n + t_p\sigma_p^n\right)^{m_s}\right]\frac{L}{\beta^{m_s}}\right\}\right\rangle \tag{20}$$

NOTE Instantaneous failure rate λ_i in equation (19) is proportional to effective fibre length L. From Equation (20) of average failure rate λ_a, failure probability F is expressed as $\lambda_a\ t_f/(3{,}6 \times 10^{12})$, and F increases from zero and asymptotically approaches to 1 as L increases from zero to infinite. Normally the interest of discussion is a region where $F << 1$ holds, λ_a can be considered approximately proportional to L.

7.2.2 Long lengths in tension

Use several applied stresses, as a fraction of the nominal proof test stress, in the above equations for a fibre length L = 1 km. As a function of time out to 50 years, these give the instantaneous and averaged failure rate plots of Figures 2 and 3, respectively. The corresponding values are given in Table 2. (Zero time is avoided because of the singularity shown there of the averaged failure rate.)

Two points are worth noting. First, all the failure rates are almost constant over time, especially at the lower stresses. This indicates an almost linear increase in total cumulative failures with time. Secondly, and because of this, there is little practical difference in the values between the instantaneous and averaged failure rates.

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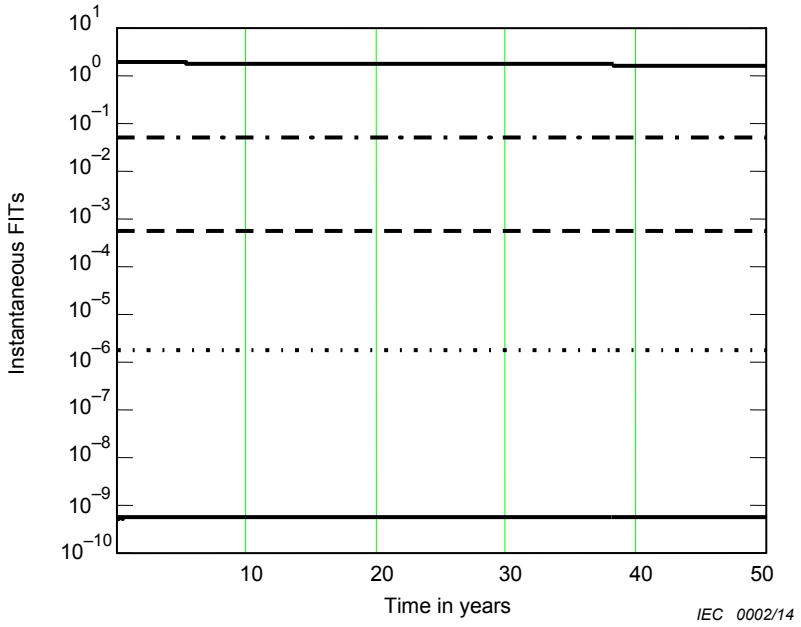

Figure 2 – Instantaneous FIT rates of 1 km fibre versus time for applied stress/proof test stress percentages (bottom to top): 10 %, 15 %, 20 %, 25 %, 30 %

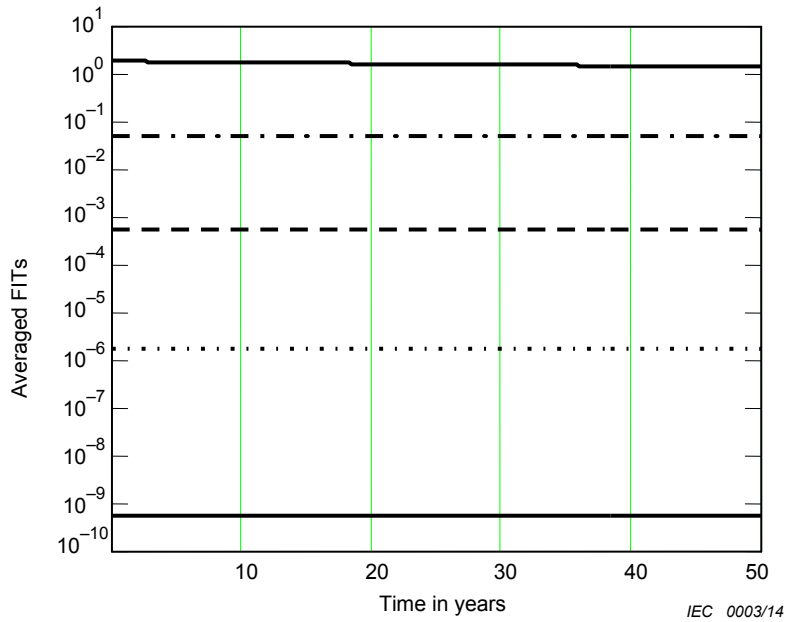

Figure 3 – Averaged FIT rates of 1 km fibre versus time for applied stress/proof test stress percentages (bottom to top): 10 %, 15 %, 20 %, 25 %, 30 %

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