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Selected illustrations of full factorial experiments with four factors

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National foreword

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TECHNICAL REPORT

ISO/TR 29901

First edition
2007-11-01

Selected illustrations of full factorial experiments with four factors

Illustrations choisies de plans d'expérience factoriels complets à quatre facteurs

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Foreword

ISO (the International Organization for Standardization) is a worldwide federation of national standards bodies (ISO member bodies). The work of preparing International Standards is normally carried out through ISO technical committees. Each member body interested in a subject for which a technical committee has been established has the right to be represented on that committee. International organizations, governmental and non-governmental, in liaison with ISO, also take part in the work. ISO collaborates closely with the International Electrotechnical Commission (IEC) on all matters of electrotechnical standardization.

International Standards are drafted in accordance with the rules given in the ISO/IEC Directives, Part 2.

The main task of technical committees is to prepare International Standards. Draft International Standards adopted by the technical committees are circulated to the member bodies for voting. Publication as an International Standard requires approval by at least 75 % of the member bodies casting a vote.

In exceptional circumstances, when a technical committee has collected data of a different kind from that which is normally published as an International Standard ("state of the art", for example), it may decide by a simple majority vote of its participating members to publish a Technical Report. A Technical Report is entirely informative in nature and does not have to be reviewed until the data it provides are considered to be no longer valid or useful.

Attention is drawn to the possibility that some of the elements of this document may be the subject of patent rights. ISO shall not be held responsible for identifying any or all such patent rights.

ISO/TR 29901 was prepared by Technical Committee ISO/TC 69, *Applications of statistical methods*.

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Introduction

The Six Sigma and international statistical standards communities share a philosophy of continuous improvement and many analytical tools. The Six Sigma community tends to adopt a pragmatic approach driven by time and resource constraints. The statistical standards community arrives at rigorous documents through long-term international consensus. The disparities in time pressures, mathematical rigor and statistical software usage have inhibited exchanges, synergy and mutual appreciation between the two groups.

The present document takes one specific statistical tool (full factorial designs with four factors, 2^4 designs) and develops the topic somewhat generically (in the spirit of International Standards) but then illustrates it through the use of five detailed and distinct applications. The generic description focuses on the commonalities across 2^4 designs. These commonalities hold more generally for arbitrary numbers of factors, but a value of four was chosen for this Technical Report. The annexes containing the five illustrations follow the basic framework but also identify the nuances and peculiarities in the specific applications. Each example offers at least one “wrinkle” to the problem, which is generally the case for real Six Sigma applications. It is thus hoped that practitioners can identify with at least one of the five examples, if only to remind them of the basic material on factorial designs that was encountered during their Six Sigma training. Each of the five examples is developed and analysed using statistical software of current vintage. The explanations throughout are devoid of mathematical detail — such material can be readily obtained from the many design and analysis of experiments textbooks available (such as those given in the Bibliography).

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Selected illustrations of full factorial experiments with four factors

1 Scope

This Technical Report describes the steps necessary to specify, to use and to analyse 2^4 full factorial designs through illustration, with five distinct applications of this methodology.

Depending on the application, a number of factors other than four may be considered in the experiment.

NOTE 1 Each of these five illustrations is similar in that sufficient resources were available to implement the design. Other commonalities among the five examples are noted (e.g. study objective, two levels for factors, response variable(s), factors effecting the response). The individual illustrations have some salient features that are distinct such as presence/absence of repetitions, centre points, interactions, or different types of response variables. Each illustration takes place in a different environment such as marketing, software, manufacturing, telecommunications and chemical processing.

NOTE 2 For the purposes of this Technical Report, the selection of four factors with two levels (aside from centre points) was made in advance. Furthermore, the detailed use of response surface designs as a follow-up or augmentation of the existing designs was excluded from this Technical Report, although their use is noted in some of the illustrations. Likewise, Taguchi designs and blocking designs were not included.

NOTE 3 Full factorial experiments are often employed by individuals (so-called “black belts” or “green belts”) associated with Six Sigma methods. Six Sigma methods are concerned with problem solving and continuous improvement. A full factorial experiment with four factors is one of many tools available to Six Sigma practitioners, but hitherto has not been addressed in detail in ISO International Standards.

2 Normative references

The following referenced documents are indispensable for the application of this document. For dated references, only the edition cited applies. For undated references, the latest edition of the referenced document (including any amendments) applies.

ISO 3534-1:2006, *Statistics — Vocabulary and symbols — Part 1: General statistical terms and terms used in probability*

ISO 3534-2, *Statistics — Vocabulary and symbols — Part 2: Applied statistics*

ISO 3534-3:1999, *Statistics —Vocabulary and symbols — Part 3: Design of experiments*

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3 Terms and definitions

For the purposes of this document, the terms and definitions in ISO 3534-1, ISO 3534-2, ISO 3534-3 and the following apply.

3.1
analysis of variance
ANOVA
technique which subdivides the total variation of a response variable into meaningful components associated with specific sources of variation

NOTE Adapted from ISO 3534-3:1999, definition 3.4.

3.2
binomial distribution
discrete distribution having the probability mass function

$$P(X = x) = \frac{n!}{x!(n-x)!} p^x (1-p)^{n-x}$$

where $x = 0, 1, \ldots, n$ and with indexing parameters $n = 1, 2, \ldots$, and $0 < p < 1$.

NOTE Adapted from ISO 3534-1:2006, definition 2.46.

3.3
block
collection of experimental units more homogeneous than the full set of experimental units

NOTE Adapted from ISO 3534-3:1999, definition 1.11.

3.4
centre point
vector of factor level settings of the form $(a_1, a_2, \ldots, a_k)$, where all a_i equal 0, as notation for the coded levels of the factors

NOTE Adapted from ISO 3534-3:1999, definition 1.36.

3.5
design matrix
matrix with rows representing individual treatments (possibly transformed according to the assumed model) which can be extended by deduced levels of other functions of factor levels (interactions, quadratic terms, etc.) but are dependent upon the assumed model

NOTE Adapted from ISO 3534-3:1999, definition 2.7.1.

3.6
factor
predictor variable that is varied with the intent of assessing its effect on the response variable

NOTE Adapted from ISO 3534-3:1999, definition 1.5.

3.7
full factorial experiment
experiment consisting of all possible treatments formed from two or more factors, each being studied at two or more levels

NOTE Adapted from ISO 3534-3:1999, definition 2.1.

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3.8
interaction
effect for which the apparent influence of one factor on the response variable depends upon one or more other factors

NOTE Adapted from ISO 3534-3:1999, definition 1.17.

3.9
level
potential setting, value or assignment of a factor

NOTE Adapted from ISO 3534-3:1999, definition 1.6.

3.10
normal distribution
continuous distribution having the probability density function

$$f(x) = \frac{1}{\sigma\sqrt{2\pi}} e^{-\frac{(x-\mu)^2}{2\sigma^2}}$$

where $-\infty < x < \infty$ and with parameters $-\infty < \mu < \infty$ and $\sigma > 0$

NOTE Adapted from ISO 3534-1:2006, definition 2.50.

3.11
predictor variable
variable that can contribute to the explanation of the outcome of an experiment

NOTE Adapted from ISO 3534-3:1999, definition 1.3.

3.12
randomization
process used to assign treatments to experimental units so that each experimental unit has an equal chance of being assigned a particular treatment

NOTE Adapted from ISO 3534-3:1999, definition 1.29.

3.13
replication
performance of an experiment more than once for a given set of predictor variables

NOTE Adapted from ISO 3534-3:1999, definition 1.27.

3.14
split-plot design
design in which a group of experimental units (plot) to which the same level assigned to the principal factor is subdivided (split) so as to study one or more additional principal factors within each level of that factor

NOTE Adapted from ISO 3534-3:1999, definition 2.3.6.

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4 Symbols and abbreviated terms

The symbols and abbreviated terms used in this Technical Report are as follows:

y	Response variable
A, B, C, D	Factors
AB, AC, AD, BC, BD, CD	2-way interactions
ABC, ACD, BCD	3-way interactions
ABCD	4-way interactions
+1/–1	High and low settings
2^4	Four factors each with two levels
σ	Standard deviation

5 Generic description of full factorial designs

5.1 Overview of the structure of the four factor examples in Annexes A through E

This Technical Report provides general guidelines on the design, conduct and analyses of two-level full factorial designs and illustrates the steps with five distinct applications given in Annexes A through E. Each of these five examples follows the basic structure given in Table 1.

The steps given in Table 1 apply to design and analysis of experiments in general, although this Technical Report focuses on 2^4 full factorial designs. Each of the seven steps is explained in general below. Specific explanations of the substance of these steps is provided in the examples in Annexes A through E.

Table 1 — Basic steps in experimental design

1	State the overall objective(s) of the experiment
2	Describe the response variable(s)
3	List the factors that might affect the response(s)
4	Select a “full” factorial design
5	Analyse the results – Numerical summaries and graphical displays
6	Present the results
7	Perform a confirmation run

5.2 Overall objective(s) of the experiment

Experiments are conducted for a variety of reasons. The primary motivation for the experiment should be clearly stated and agreed to by all parties involved in the design, conduct, analysis and implications of the experimental effort. There may be secondary objectives which could be addressed with the full factorial experiment.

The ultimate outcome of the experiment could be to take immediate action on factor levels or to obtain a predictive model, both of which dictate some elements of the analyses.

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5.3 Response variable(s)

Associated with the objective of an experiment is a measurable outcome or performance measure. A response of interest could involve maximization (larger is better), minimization (smaller is better) or meet a target value (be close to a specified value). The response variable (denoted here by the variable y) should be intimately (if not directly) related to the objective of the experiment. For some situations, there may be multiple characteristics of interest to be considered, although there typically is a primary response variable associated with the experiment. In other cases, multiple responses must be considered; however, for purposes of this document, a single response is considered in each example.

5.4 Factors affecting the response(s)

The response variable likely depends in some unknown way on a variety of conditions that occur or could be set in the course of generating a response variable outcome. These conditions are presumed to relate to controllable factors that may be continuous (temperature, concentration) or discrete (two assembly lines A or B, two vendors, two packaging styles, and so forth). For 2^4 experiments, we simplify the experimental design process by selecting two levels for each factor to be varied in the experiment. For discrete factors with only two possible settings, the levels of this factor are just these two settings. For continuous factors, there is discretion in choosing the two specific values. In some cases, the two settings could be the historical value and a proposed value. In other cases, the two settings could be a nominal adjustment from the historical setting. In any event, the settings should be sufficiently far removed to have an opportunity to reveal an impact subject to the inherent uncertainty, while not being so disparate that the settings are unreasonable from a practical, safety or sensibility standpoint. The setting of levels of continuous factors benefits from the domain expert collaborating on the experiment.

There may be additional factors that could impact that response variable but may be deemed less important than the chosen four factors or are too difficult or expensive to control. Finally, it is the case that the factors are to be set independently from each other. It could, however, be discovered that the factors interact (the setting of one factor impacts how a second factor affects the response).

5.5 “Full” factorial design

This classical design consists of 16 runs obtained by considering all combinations of four factors with two possible levels. Table 2 provides the basic layout in a standard order for ease of understanding. Each row of the table represents one set of experimental conditions that when run will produce a value of the response variable y. The four factors are designated as A, B, C and D. For an individual factor, the level “−1” is the “low” setting, or one of the two levels if the factor is categorical. The level “+1” is the “high” setting, or the other level of the categorical factor. The column “y” is a placeholder for the response value once a run has occurred.

In addition to providing the explicit 16 experimental runs to be conducted, Table 2 provides an example of a randomized run order. The experiment should not be run in the standard order (for example, an increasing trend in the response could be confused with the effect of factor D on the response). The final two columns provide abbreviated names for the 16 runs. The first name coincides with the “+” or “−” levels of the factors given in the order for ABCD. The second naming convention includes a lower case letter for each factor at its high level. By convention, the four settings at the low level are designated as “(1)” since otherwise the abbreviation would be null.

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Table 2 — Layout of a generic 2^4 full factorial design

Row number	A	B	C	D	y	Run order	Name of run	Alternate name of run
1	–1	–1	–1	–1	y_1	6	– – – –	(1)
2	+1	–1	–1	–1	y_2	14	+ – – –	a
3	–1	+1	–1	–1	y_3	4	– + – –	b
4	+1	+1	–1	–1	y_4	11	+ + – –	ab
5	–1	–1	+1	–1	y_5	9	– – + –	c
6	+1	–1	+1	–1	y_6	2	+ – + –	ac
7	–1	+1	+1	–1	y_7	3	– + + –	bc
8	+1	+1	+1	–1	y_8	1	+ + + –	abc
9	–1	–1	–1	+1	y_9	8	– – – +	d
10	+1	–1	–1	+1	y_{10}	13	+ – – +	ad
11	–1	+1	–1	+1	y_{11}	7	– + – +	bd
12	+1	+1	–1	+1	y_{12}	10	+ + – +	abd
13	–1	–1	+1	+1	y_{13}	15	– – + +	cd
14	+1	–1	+1	+1	y_{14}	16	+ – + +	acd
15	–1	+1	+1	+1	y_{15}	5	– + + +	bcd
16	+1	+1	+1	+1	y_{16}	12	+ + + +	abcd

In the situation with all four factors being continuous (quantitative), some experimenters elect to run additional “centre” points. The levels of the centre point are at the midpoint of the two levels of each factor. The inclusion of centre points facilitates statistical testing of effects, using the variability of the responses at the centre points as a guideline. It also provides the means to test for non-linearity (curvature) of the response.

In the situation where a particular factor is difficult or expensive to change from one level to the other, the experiment could be conducted in “blocks”, one block for each level of the difficult factor.

One final situation concerns replication of the runs in the design. Multiple replications at each experimental setting accommodate estimates of the overall inherent variability which can then be pooled for statistical testing purposes.

5.6 Analyse the results — Numerical summaries and graphical displays

At the completion of the conduct of the experiment, the y_i values would be replaced by the actual observed responses. Many existing statistical software packages exist to facilitate the generation of output to aid in the understanding of the results of the experiment. Of immediate concern is the determination of the impact of the four factors individually on the response variable. Thus, the main effects for A, B, C and D are to be estimated as well as the following interaction terms:

— two-way: AB, AC, AD, BC, BD, CD;

— three-way: ABC, ABD, ACD, BCD;

— four-way: ABCD.

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In addition to the actual estimates, it is useful to arrange the estimated effects from largest to smallest in the form of a Pareto Chart. The effects can also be presented on a normal or half-normal plot to identify the stronger effects. Depending on the inclusion of centre points or replication, the experimental error can be estimated directly and in turn the standard error of the effects can be determined. In the absence of these experimental runs, the experimental error can be estimated indirectly by presuming that three-way and four-way interactions are negligible. Effects plots, interaction plots and residual plots are also generally considered in assessing the results of an experiment. These are illustrated in Annexes A through E.

5.7 Present the results

Frequently, the purpose of the experiment is to develop a predictive model so as to explore alternate settings of the factors. Contour plots are available from most software packages. Moreover, with a predictive model, tentative consideration of optimal settings can be identified. The predictive model will consist of a function (typically linear) of the estimated effects and possibly interactions. Alternate mathematical models may be envisaged depending on examination of the residuals (collection of predictive values minus observed values).

5.8 Perform confirmation runs

Follow-up experiments may prove useful to demonstrate that the lessons learned from the 2^4 full factorial experiments are verified in subsequent runs. A natural follow-on experiment could be to identify a promising direction in which to adjust the factors for improved performance in the response variable.

6 Description of Annexes A through E

6.1 Comparing and contrasting the examples

Five distinct examples of 2^4 full factorial designs are illustrated in Annexes A to E. Each of these examples follows the same general template as given in Table 1 and follows a version of the standard design given in Table 2.

6.2 Experiment summaries

Table 3 summarizes the five examples detailed in the annexes and indicates aspects of the analyses which were unique to each experiment.

Table 3 — Experiment summaries found by annex

Annex	Experiment	Problem-specific aspects
A	Solder bars	Mixture of discrete and continuous factors; repetitions; important 2-way interaction
B	Direct mail campaign	Proportion response variable, standard errors based on binomial distribution
C	Button tactility	Centre points; curvature in response
D	PVC formulation optimization	Split-plot; centre points; contour plots
E	Genetic algorithms	Randomized order not necessary; set up for interim analyses; replication; dispersion effect

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Annex A
(informative)

Solder bar experiment[1)]

A.1 General

The material solder can be produced in a number of forms. One of the most common is a bar of solid solder. The bars are sold by mass, namely 0,5 kg, 1,0 kg and 2,0 kg.

A.2 Overall objective for the experiment

The process had recently been relocated to a new site and subsequently, on the underside of the bars there were a large number of “rosettes” (small pits on the surface of the solder bar). This led to numerous customer complaints, customers assuming that the solder was of an inferior standard. The current level of rosettes on bars was assessed to be about 30 per bar.

The operational staff had tried over several months various “one-factor-at-a-time” experiments, none of which produced a large enough improvement for the producer to say to their customers that they had solved the problem. It was decided to design and then run an experiment to understand the factors responsible for the defect and then how to manage the process so as to minimize the number of rosettes.

A.3 Description of the process

Solder bars are produced by pouring molten solder into moulds pre-selected according to the target mass of the bars to be produced.

Ingots of solder are firstly melted in an electric furnace at about 290 °C. An operator then produces the bars by filling a “kettle” with the molten solder and then by pouring the solder from the kettle into moulds. A kettle is similar to the kitchen utensil of the same name but with extra spouts, thus enabling several bars to be poured simultaneously.

The bars are cast upside down so the bottom of each bar is uppermost and open to the atmosphere. The moulds are arranged in banks on a table with water-cooling integrated into it that can be turned on or off. Before casting, the moulds can be “smoked”. This is a layer of carbon applied with an oxyacetylene torch.

After a short period of time during which the bars solidify, they are de-moulded, stacked and then packed.

A.4 Response variable

A.4.1 Choice of variable

The response chosen for the experiment was the average number of rosettes counted on the surface of the bars. The objective was to minimize the average number of rosettes.

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1) This example has been kindly donated by Cookson Electronics (Fry's Metals Glasgow).

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A.4.2 Measurement of the response variable

Approximately 160 bars were produced in each experimental "run". The number of rosettes was counted across all of the solder bars and the arithmetic mean of the number of rosettes per bar calculated for each experimental run. This became the output for that experimental run.

A.4.3 Relationship of the response variable to the objective of the experiment

The mean number of rosettes per bar is directly linked to the objective of the experiment.

A.5 Factors affecting the response

A.5.1 Description of each factor (continuous/discrete) to be varied

The factors chosen to be varied within the experiment were determined using the knowledge of the production operators and the technical staff. These were:

A: the casting temperature of the molten solder;

B: water-cooling, applied or not;

C: the pouring rate of the molten solder into the moulds; and

D: whether the moulds were smoked or not.

The experiment was to be run using these four factors each at two levels.

Factor A was clearly a factor that could be adjusted to any given temperature. Factor C was, in theory, one that could be varied as a continuous variable. However, in practice, it was handled as a categorical factor and the rate was either "Normal" or "Maximum".

The other two factors were categorical. Water cooling, factor B, was either "Off" or "On" and the moulds, factor D, were either not smoked "No" or smoked "Yes".

A.5.2 Selection of levels (related to size of effect to be determined)

The factors used in the experiment and their associated levels are given in Table A.1.

Table A.1 — Factors and their associated levels

Factor	Level 1	Level 2
A: Casting temperature (°C)	260	320
B: Water cooling	Off	On
C : Pouring rate	Normal	Maximum
D: Mould conditioning	No	Yes

The casting temperatures selected were determined to be the extremes that would be considered during production. This was a result of discussions with the technical and metallurgical staff.

The levels for the remaining factors were deemed to be discrete, e.g. "On" or "Off".

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Prior to the experiment, it was really not known if the selected factors would have any effect on the response, and so this might be regarded as a “screening” experiment. The considered opinion of the technical department was that these factors were very likely to be linked to the response and that the levels chosen for the casting temperature were wide enough to generate an observable change in the response.

A.5.3 Other factors noted but not incorporated due to issues with controllability or relevance

Other factors that might have been considered, but were not included in the experiment, are given in Table A.2.

Table A.2 — Factors not included in the experiment

Factor	Reason for exclusion
Air temperature	Air temperature was not regarded as important to the response and the factory was not temperature controlled and this would have been very difficult to control.
Humidity	Considered irrelevant and the factory did not posses air conditioning so therefore it would have been impossible to control.
Air cleanliness	The atmosphere within the factory was naturally smoky and it would have been impossible to control the level of cleanliness.
Operator	There was only one operator involved with this process and so the inclusion of different operators for this experiment was seen as irrelevant.
Day	The day of the week was regarded as irrelevant for this experiment.

A.6 Full factorial design

A.6.1 Design matrix (standard order, run order)

The design selected was a full factorial that allowed for all interactions to be examined. Table A.3 shows the design.

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Table A.3 — Design matrix

A: Casting temperature °C	B: Water cooling	C: Pouring rate	D: Mould conditioning	Standard order	Run order
320	On	Maximum	No	8	1
320	Off	Maximum	No	6	2
260	On	Maximum	No	7	3
260	On	Normal	No	3	4
260	On	Maximum	Yes	15	5
260	Off	Normal	No	1	6
260	On	Normal	Yes	11	7
260	Off	Normal	Yes	9	8
260	Off	Maximum	No	5	9
320	On	Normal	Yes	12	10
320	On	Normal	No	4	11
320	On	Maximum	Yes	16	12
320	Off	Normal	Yes	10	13
320	Off	Normal	No	2	14
260	Off	Maximum	Yes	13	15
320	Off	Maximum	Yes	14	16

The experiment was randomized and the column headed “Run order” was the order in which the runs were performed during the experiment. The column “Standard order” specifies where the particular factor combination would be found in the “design matrix” for the 4-factor 2-level design.

A.6.2 Centre points

Centre points were not selected for this experiment, partly because three of the four factors were taken as categorical (binary) factors, making centre points inconvenient to arrange.

A.6.3 Replication and repetition

The factory could not afford any more experimental time than that needed to conduct the 16 run experiment shown above. Therefore, there was no replication of any of the experimental runs. However, once an experimental run had been set up, about 160 bars were produced, providing abundant repetition.

Repetition is important to overcome effects of measurement uncertainty and to improve the reliability of the analysis. The decision taken to average the number of rosettes was seen as appropriate in this case. At other times different decisions might be taken, e.g. to calculate a standard deviation from the repeated measurements for each replicated run. These repetitions provide the analyst with information about factors that might influence the process variability.

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