

SEMI C10-1109

GUIDE FOR DETERMINATION OF METHOD DETECTION LIMITS

This Standard was technically approved by the Liquid Chemicals Global Technical Committee. This edition was approved for publication by the global Audits and Reviews Subcommittee on September 4, 2009. Available at www.semi.org in November 2009; originally published in June 1998; previously published March 2005.

1 Purpose

1.1 To provide a minimal set of guidelines for the quantitative determination of a method detection limit (MDL) from data supporting a SEMI Process Chemicals or Gases specification.

2 Scope

2.1 This guide applies to trace contaminants specified in SEMI Process Chemicals or Gases standards and guidelines. All relevant trace contaminants should have an MDL determined from a regression analysis of a calibration curve that is equal to, or less than, their specifications. This guide is intended for use in both establishing new specifications within SEMI as well as verification of performance to SEMI specifications.

NOTICE: SEMI Standards and Safety Guidelines do not purport to address all safety issues associated with their use. It is the responsibility of the users of the Documents to establish appropriate safety and health practices, and determine the applicability of regulatory or other limitations prior to use.

3 Referenced Standards and Documents

3.1 SEMI Standards and Safety Guidelines

SEMI C16 — Guide for Precision Reporting/Data Traceability

3.2 Other Document¹

Applied Regression Analysis, 3rd Edition, Norman R. Draper and Harry Smith, John Wiley and Sons, © 1998

NOTICE: Unless otherwise indicated, all documents cited shall be the latest published versions.

4 Terminology

4.1 None.

5 Boundary Conditions

NOTE 1: A series of boundary conditions is required of the data from which the MDL is to be determined.

5.1 Data should be collected on at least two standards at different concentration levels, not including the blank.

5.2 The concentration levels investigated must either span the relevant specification or include it as a level. For this purpose, the calibration range can be adjusted for instrument sensitivity by pre-concentration or dilution, if applicable.

5.3 A minimum of three sample determinations should be taken on each concentration level of the standard investigated.

5.4 Matrix Effects

5.4.1 The blank and the standards should be matrix-matched with the sample when testing a specification and run under the same conditions, both during calibration and sample analysis.

5.4.2 If external standards in a different matrix are used for calibration, the user must compensate for matrix effects using suitable internal standards or demonstrate the absence of matrix effects.

5.5 Where applicable, this guide supersedes the earlier related SEMI Guide, SEMI C16.

5.6 The frequency of the MDL determination should be part of the quality assurance program for the laboratory.

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6 Procedure

NOTE 2: The determination of the MDL should be performed under the same conditions that samples will normally be run. All appropriate precautions to avoid contamination should be followed.

6.1 An MDL will be the average of multiple MDL determinations taken over at least 2 days. § 6 describes how to obtain a single MDL estimate. § 7 describes how many MDL estimates are required.

6.2 *Reagents and Standards* — Reagents and standards used should be of the same high-purity as used in the analysis of samples. Accurate standard solutions of trace contaminants are needed for the preparation of the calibration standards. Commercially available standard solutions are suitable. These solutions should be traceable to NIST standards. Working standard solutions should be prepared on the day of use by dilution of the stock standard solution. Standards and blanks should be matrix-matched to the sample to be analyzed when possible.

6.3 Operating Conditions

6.3.1 *Instrumental* — Principles of instrumental analysis are provided within many monographs. No general operating conditions are given here since these will vary with the instrument type and design; consequently, the manufacturers manual should be followed.

6.3.2 *Standard and Sample Preparation* — With certain methods, the achievable MDL can be improved by pre-concentration. Some methods require matrix dilution to run some analyses and may also affect the MDL.

6.3.3 *Calibration* — Calibrate the instrument for all specified trace contaminants using measurement and preparation protocols identical to those used in sample preparation and measurement, wherever appropriate. The calibration data structure used to determine the MDL should be as close to identical as possible to the data structure normally used for calibration in the laboratory. Minimum data requirements should be determinations at, at least, two concentration levels (standards), each sampled 3 times. The lowest concentration standard should be at, or below, the specification and give a measurable signal. The blank may be used in the calculation of the MDL if its variability is judged to be representative of that of a very low-level standard. All instrument response data used in the analysis should be measurable. The calibration range can be adjusted for instrument sensitivity by pre-concentration or dilution to match with how the samples are analyzed. Use the data collected to calculate the MDL using the formulas in the next section.

6.4 Quantification of the MDL

6.4.1 The MDL is calculated by using the results from a *regression analysis* of the calibration data to obtain a 3 sigma equivalent (in probability) upper confidence limit of individual measurements. Two alternative computational methods are provided for linear calibration models. One provides the MDL based on an ordinary least squares (OLS) regression analysis; the other on a weighted least squares (WLS) based regression analysis. These two computational alternatives **do not** provide the same MDL. The OLS algorithm is appropriate when signal uncertainty remains relatively constant over the window of calibration; otherwise, the WLS algorithm is more appropriate. A third alternative allows the use of similar regression-based approaches for MDL determination in the presence of a more complex calibration model (e.g., nonlinear, multivariate), or when distributional assumptions of the other alternatives are not appropriate. Many software packages perform regression analysis, and their use is recommended.

6.4.2 Statistical Definitions

6.4.2.1 *Method Detection Limit (MDL)* — The level at which the errors in the *measurement method* become large enough such that the preset maximum acceptable risk of seeing the quantified level, when none of the contaminant in question is present in the sample, is exceeded.

6.4.2.2 *Risk* — This guide uses 0.13% as the maximum acceptable risk. This is the probability of observing a given result from a normal distribution that is 3 or more standard deviations above the average. Risk is set on a per-contaminant basis.

6.4.2.3 *Calibration Curve* — An estimate of the relationship between concentration and instrument response (signal intensity). A line, which has not been constrained to pass through the origin, is implicitly assumed in the subsequently provided formulae.

6.4.2.4 *Regression Analysis* — A curve-fitting technique from which the calibration curve can be estimated.

6.4.2.5 *Ordinary Least Squares (OLS)* — A curve-fitting criterion which, for a given calibration model, minimizes.

$$\sum_{i=1}^n (Y_i - \text{Predicted } Y_i)^2 \quad (1)$$

Appropriate use of this criterion implicitly assumes that, on average, each determination is made with equal reliability.

6.4.2.6 *Weighted Least Squares (WLS)* — A curve-fitting criterion which, for a given calibration model, minimizes.

$$\sum_{i=1}^n w_i (Y_i - \text{Predicted } Y_i)^2 \quad (2)$$

where, w_i is the weight assigned to the i^{th} data point.

Appropriate use of this criterion implicitly assumes that all w_i are strictly inversely proportional to each point's standard deviation (measure of variation).

6.4.2.7 *T-statistic* — Student's t is used instead of the Z-statistic (normal distribution) when the standard deviation is estimated from relatively small quantities of data. It is used herein to explicitly control the risk at 0.13%, regardless of sample size.

- X_s — The concentrations of the standards used in quantifying the MDL.
- Y_s — The instrument's response (signal intensity) to each of the X_s in question.

6.4.3 *Calculations — OLS and Linear Calibration Model*

6.4.3.1 A line, which is not constrained to pass through the origin, is used as the calibration model. OLS is used to estimate the model. The MDL is located by determining the 3 sigma equivalent Upper Confidence Limit at $X = 0$ and using a linear calibration model to convert this result into the corresponding concentration (MDL).

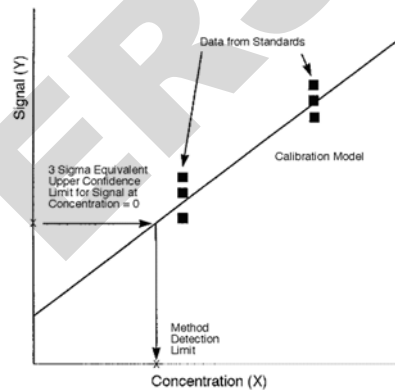


Figure 1
Graphical Visualization of MDL Determination Process

$$MDL = \frac{(UCL - b)}{m} \quad (3)$$

where:

m = slope determined by OLS analysis (Equation 4).

b = intercept determined by OLS analysis (Equations 5–8).

UCL = 3 sigma equivalent Upper Confidence Limit at $X = 0$ (Equation 8).

$$m = \frac{SS_{xy}}{SS_{xx}} \quad (4)$$

where SS stands for Sum of Squares, and

$$\begin{aligned} SS_{xy} &= \sum_i (X_i - \bar{X})(Y_i - \bar{Y}) \\ &= \sum_i X_i Y_i - \frac{(\sum_i X_i)(\sum_i Y_i)}{n} \end{aligned} \quad (5)$$

where n = total number of observations and i is an index which ranges from 1 to n by 1 in the summations, and

$$\begin{aligned} SS_{xx} &= \sum_i (X_i - \bar{X})^2 = \sum_i (X_i^2) - \frac{(\sum_i X_i)^2}{n} \\ b &= \bar{Y} - m\bar{X} \end{aligned} \quad (6)$$

where:

$$\bar{X} = \frac{\sum_i X_i}{n} \quad (7)$$

and,

$$\begin{aligned} \bar{Y} &= \frac{\sum_i Y_i}{n} \\ UCL &= b + t_{n-2, 0.0013} \left(1 + \frac{1}{n} + \frac{(\bar{X})^2}{SS_{xx}} \right)^{1/2} s \end{aligned} \quad (8)$$

where: $t_{n-2, 0.0013}$ is a t-statistic (from Table 1) with $n - 2$ degrees of freedom and 0.0013 as the desired risk of detecting a false positive signal (one-sided, 3 sigma equivalent) and s = standard deviation of regression model.

$$\begin{aligned} &= \left(\frac{\sum_i (Y_i - Y_i^*)^2}{n-2} \right)^{1/2} \end{aligned} \quad (9)$$

where: $Y_i^* = mX_i + b$

Table 1 3-Sigma Equivalent t-Table

$n-2$	t	$n-2$	t	$n-2$	t
4	6.62	10	3.96	16	3.54
5	5.51	11	3.85	17	3.51
6	4.90	12	3.76	18	3.48
7	4.53	13	3.69	19	3.45
8	4.28	14	3.64	20	3.42
9	4.09	15	3.59		

6.4.3.2 Such analyses should be performed by using a spreadsheet or computer program. It is not recommended to do them by hand. The previous equations neither require nor prevent use of data from blank quantification. In order to use blank data in the MDL quantification with OLS, the blank should be measurable, be likely to give a response which is consistent with the pattern in the other calibration data, and provide a similar level of variability to that obtained from the investigated standards.